Practical Session 3

Statistical graphics for quantitative variables

In this session, we can analyse a discrete and a continuous variable from our class questionnaire. The necessary techniques are illustrated using some of the data from the theory class examples

1. Discrete data example

In the theory class we have used the following data set of times voted by a group of Madrileños.

Times	3	3	3	4	1	2	4	5	2	3	1	1	3	8	4	1	3	4	2	5	0	0	5	4	2	1	2	3	3	2
voted	1	4	3	2	3	5	0	6	3	1	3	5	4	1	4	1	2	4	4	3	3	0	7	2	2	1	3	4	2	2

Before trying to set up a frequency table, it is useful to first calculate minimum and maximum vales of the data (to know which values to use for the table). This can be done using the MIN and MAX commands.

Then we can set up a column of the different values of the table. (The easiest way is typing the first two values and dragging down). Then, as in the previous practical, we can use the COUNTIF command to calculate the frequencies of each value of the data. Remember to use the dollar trick to fix the data!

Times	Absolute
voted	frequency (n)
0	4
1	10
2	12
3	15
4	11
5	5
6	1
7	1
8	1
>8	0

As in the previous practical, we can calculate the sum of the data and the relative frequencies. This gives the following frequency table.

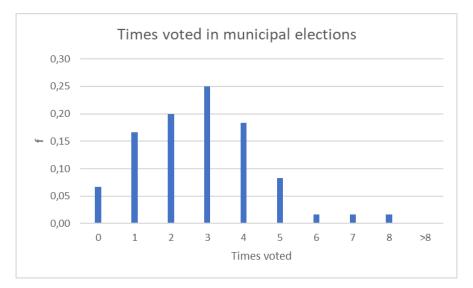
		Relative
Times	Absolute	frequency
voted	frequency (n)	(f)
0	4	0.07
1	10	0.17
2	12	0.20
3	15	0.25
4	11	0.18
5	5	0.08
6	1	0.02
7	1	0.02
8	1	0.02
>8	0	0.00
TOTAL	60	1.00

As we have discrete data, we can augment the table with cumulative frequencies. Assuming that the values 4 and 0.07 above are in cells **B2** and **C2** respectively, then we can set **D2** = **B2** and **E2** = **C2** and then **D3** = **D2**+**B3** and **E3** = **E2**+**C3** and drag down. Note that it does not make sense to include values in the TOTAL file for cumulative frequencies.

Times	Absolute	Relative	Cumulative	Cumulative relative
voted	frequency (n)	frequency (f)	frequency (N)	frequency (F)
0	4	0,07	4	0,07
1	10	0,17	14	0,23
2	12	0,20	26	0,43
3	15	0,25	41	0,68
4	11	0,18	52	0,87
5	5	0,08	57	0,95
6	1	0,02	58	0,97
7	1	0,02	59	0,98
8	1	0,02	60	1,00
>8	0	0,00	60	1,00
TOTAL	60	1,00		

2. Drawing a bar chart for discrete data.

As in the previous practical, we can use the Bar Chart Graphics option to construct the chart. Here however, we should adjust the bar width to its thinnest value, to show that the bar represents the number of data at an individual value. We can construct the bar chart with individual (or cumulative) frequencies. To construct the graph, it is easiest to just select the frequency values and then correct the labels later.



What features can you observe in your constructed graph? What are typical values of the data? Are the data symmetric or asymmetric? Do any data look unusual or atypical?

3. Constructing a frequency table for continuous data.

Yearly spending of different town halls (€)

11457973896 59003 861655342893844 61536 90628 495015676778063 87750 82409 10766460479 88872 66325 782683836082436 83531 8136463210 112842 56206 59052 526604500091562 66308 503977996465369 71803 60108 49264

When we decide on the bar intervals to use, in order to construct the frequency table, we can use the COUNTIFS (CONTAR.SI.CONJUNTO) function.

For example, if our data are in cells A1: I4 and we wish to calculate the number of data greater than 30 and less than or equal to 45, we can use the command

COUNTIFS(A1:I4;">30";A1:I4;"<=45").

Even faster, if the interval limits are in cells K1 and L1, we could write:

```
COUNTIFS(A1:I4;">"&K1;A1:I4;"<="&L1).
```

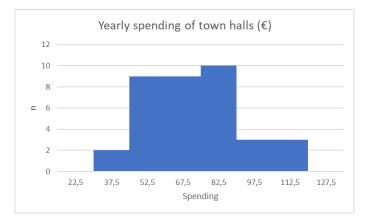
The above formula could easily be dragged down.

Yearly spending (€)	Absolute frequency
≤ 30	0
(30,45]	2
(45,60]	9
(60,75]	9
(75,90]	10
(90,105]	3
(105,120]	3
> 120	0
Total	36

Lowerlimit	Centre	Upper limit			Cumulative frequency (N)	Cumulative relative frequency (F)
15	22,5		0	0,00	0	0,00
30	37,5	45	2	0,06	2	0,06
45	52,5	60	9	0,25	11	0,31
60	67,5	75	9	0,25	20	0,56
75	82,5	90	10	0,28	30	0,83
90	97,5	105	3	0,08	33	0,92
105	112,5	120	3	0,08	36	1,00
120	127,5	135	0	0,00	36	1,00
	Total		36	1,00		

It is useful to show columns for the left and right-hand side and centre of each bar for constructing the full frequency table and corresponding graphics.

To construct the frequency histogram, we mark the frequency column and then use the bar chart graphics option as for discrete data. We then need to adjust the gaps between bars to 0 and relabel the x axis appropriately.



To construct a frequency polygon, we can use the line graph instead of the bar chart graphic.



4. Constructing a variable width histogram.

We will not deal with this problem in the practical class as it is non-trivial in Excel. A webpage explaining how to do this (in Excel 2016) is available <u>here</u>.

Note that most statistical packages always construct a relative frequency histogram defining height as frequency/width.